

INTRODUCTION

Reliable vehicle tracking from remote sensing data often requires robust state estimation across widely varying temporal resolutions. In this work, we propose a physics-informed attentive neural process (PI-AttNP) for multi-scale vehicle tracking that explicitly integrates simplified kinematic models as structural priors within a neural process framework. We benchmark this estimation approach on both real-world ship-tracking Automatic Identification System (AIS) and aeroplane Automatic Dependent Surveillance-Broadcast (ADS-B) datasets on various time scales spanning a queried time of two minutes to several hours. We compare our estimator with state-of-the-art baselines and obtain promising results.

PROBLEM STATEMENT

In this study, the objective is to learn nonlinear, coupled vector field f that represents time-varying vehicle dynamics in the following discrete-time transitional model:

$$x_{k+1} = f(\mathcal{X}, \mathcal{U}, \Delta, \Xi, \delta\mathcal{X})$$

We desire to approximate nominal dynamics f with learned representation f_Γ with neural process parameters Γ that uses *inferred*, *physics* model $g^*(\mathcal{X}, \mathcal{U}, \Delta) \in \mathcal{G} = \{g_1, g_2, \dots, g_k\}$ through the following implicit prediction scheme:

$$f_\Gamma = g^*(\mathcal{X}, \mathcal{U}, \Delta) + NN(\mathcal{X}, \mathcal{U}, \Delta|\Gamma)$$

Such that $f_\Gamma \approx f$ and no knowledge of $\Xi, \delta\mathcal{X}$

Contextual State Vector: $\mathcal{X} = \{x_{k-C}, \dots, x_{k-1}, x_k\}$

Contextual Input Vector: $\mathcal{U} = \{u_{k-C}, \dots, u_{k-1}, u_k\}$

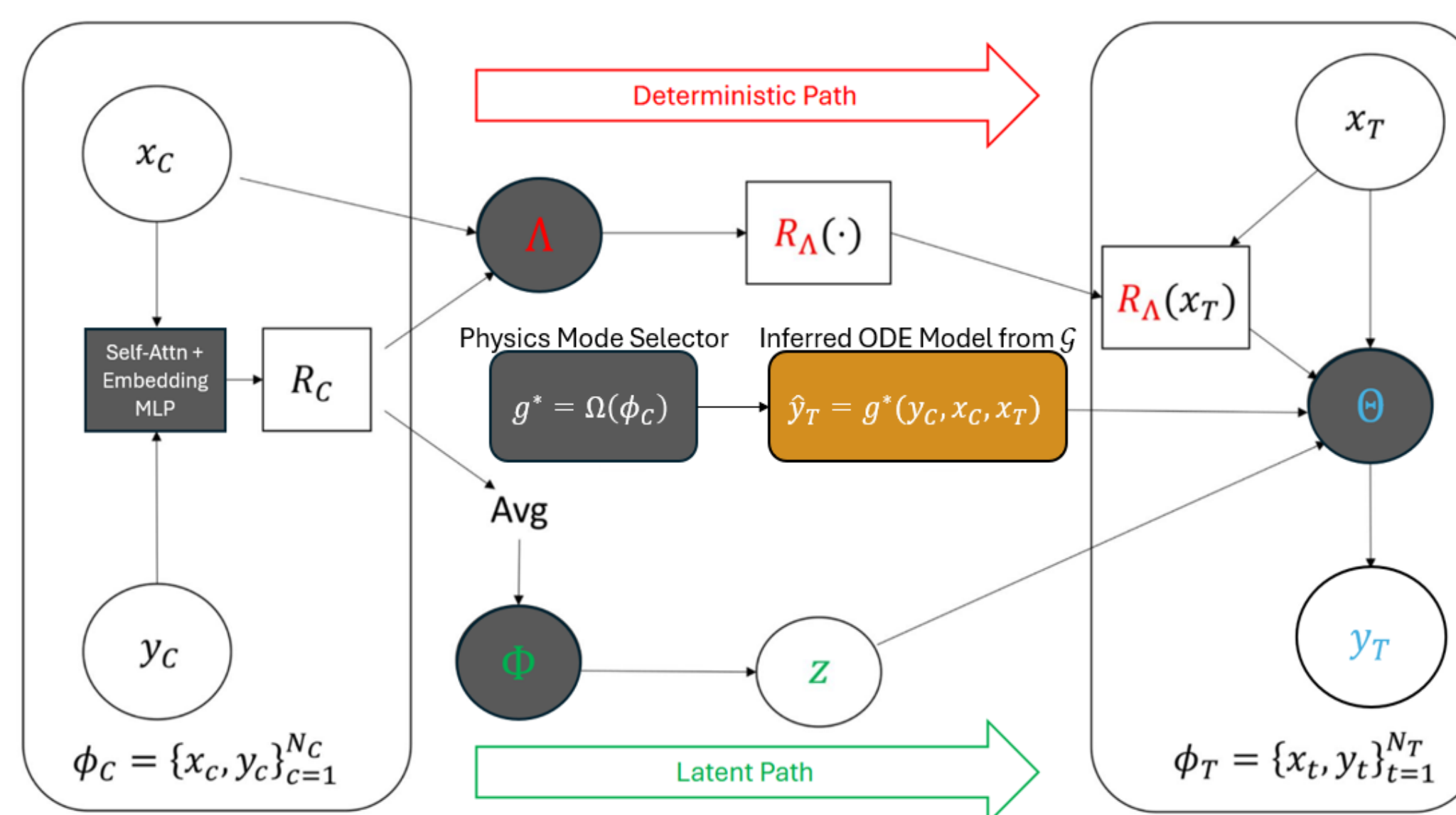
Time Step Vector: $\Delta = \{\Delta k - C, \dots, \Delta k - 1, \Delta k\}$

Sensor Noise Vector: $\Xi = \{\xi_{k-C}, \dots, \xi_{k-1}, \xi_k\}$

State Disturbance Vector: $\delta\mathcal{X} = \{\delta x_{k-C}, \dots, \delta x_{k-1}, \delta x_k\}$

Distribution Statement A. Approved for public release; distribution is unlimited.

TECHNICAL APPROACH



Computational forward diagram of the physics-informed attentive neural process (PI-AttNP). Black circles denote utilized neural networks in the NP architecture

- With the inclusion of both self and cross attention mechanisms within the forward pass of the NP, the PI-AttNP closely mimics the structure of the previous AttNP model with both *latent* and *deterministic* paths
- The *inferred ODE model* $g^*(y_C, x_C, x_T) \in \mathcal{G}$ is utilized as a physics prior that outputs apriori estimate \hat{y} given to decoder $\Theta(x_T, z, R_\Lambda, \hat{y})$
- With the inclusion of \hat{y} in decoder distribution, the NP uses the following variational lower-bound optimization:

$$p_\Theta^*, q_\Phi^*, R_\Lambda^* = \max_\Gamma \mathcal{L}(p_\Theta, q_\Phi, R_\Lambda)$$

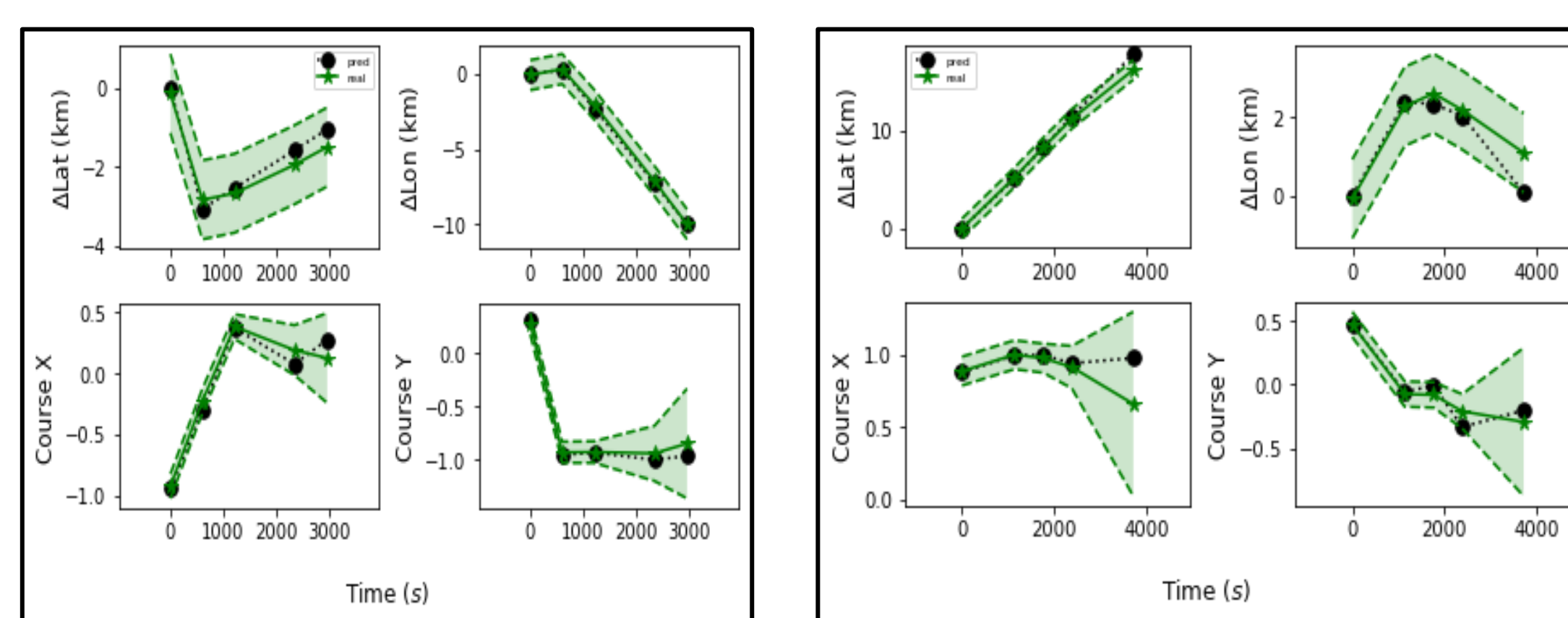
$$\log p(y_T | x_T, \phi_C) \geq \mathcal{L}(p_\Theta, q_\Phi, R_\Lambda)$$

$$= \mathbb{E}_{z \sim q_\Phi} \log p_\Theta(y_T | x_T, z, R_\Lambda, \hat{y})$$

$$-D_{KL}(q_\Phi(z | \phi_T) || q_\Phi(z | \phi_C))$$

For parameters $\Gamma = \{\Theta, \Phi, \Lambda\}$

TRAINING PROCEDURE



AIS Training Regime

$$\text{NP Input: } x_T = \begin{bmatrix} \Delta k \\ v_k \end{bmatrix}$$

$$\text{NP Output: } y_T = \begin{bmatrix} \Delta \text{Lat}_{k+1} \\ \Delta \text{Lon}_{k+1} \\ \theta_x(k+1) \\ \theta_y(k+1) \end{bmatrix}$$

Where v_k = speed over ground and θ_x, θ_y are x-y components of heading θ

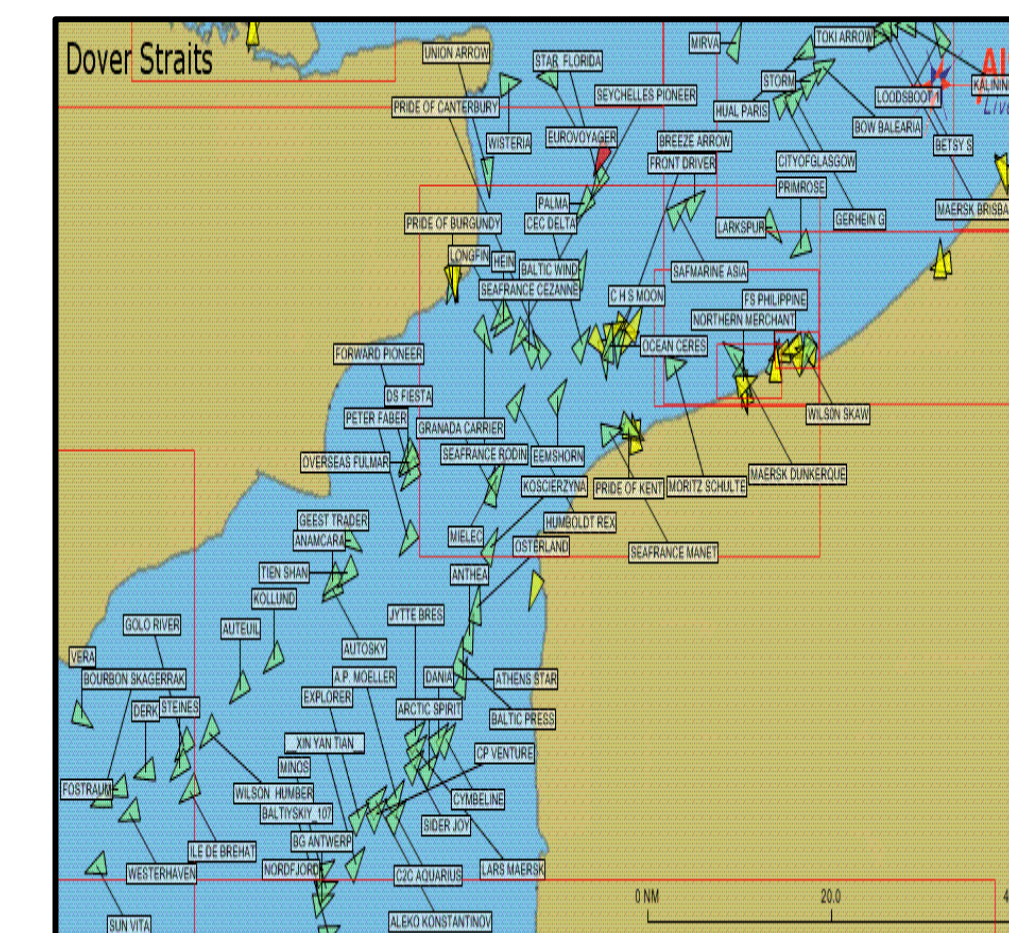
ADS-B Training Regime

$$\text{NP Input: } x_T = \begin{bmatrix} \Delta k \\ v_k \end{bmatrix}$$

$$\text{NP Output: } y_T = \begin{bmatrix} \Delta \text{Lat}_{k+1} \\ \Delta \text{Lon}_{k+1} \\ \Delta h_{k+1} \\ \theta_x(k+1) \\ \theta_y(k+1) \end{bmatrix}$$

Where v_k = longitudinal plane speed and h = altitude

PHYSICS MODELS USED IN \mathcal{G}



For AIS Dynamics

Within the AIS dataset, most dynamic transitions could be modeled as either a straight-line g_1 , constant velocity model g_2 , and stationary g_3 (i.e. $\mathcal{G} = \{g_1, g_2, g_3\}$). For g_1 and g_2 , the following ellipsoid-aware dynamics are utilized:

$$\Delta \phi_{km} = v_k \Delta k \cdot c_{ellips} \cos(\phi_k)$$

$$\Delta \lambda_{km} = v_k \Delta k \cdot c_{ellips} \sin(\phi_k)$$

$$\Delta \theta_k = \hat{\omega} \Delta k$$

Where,

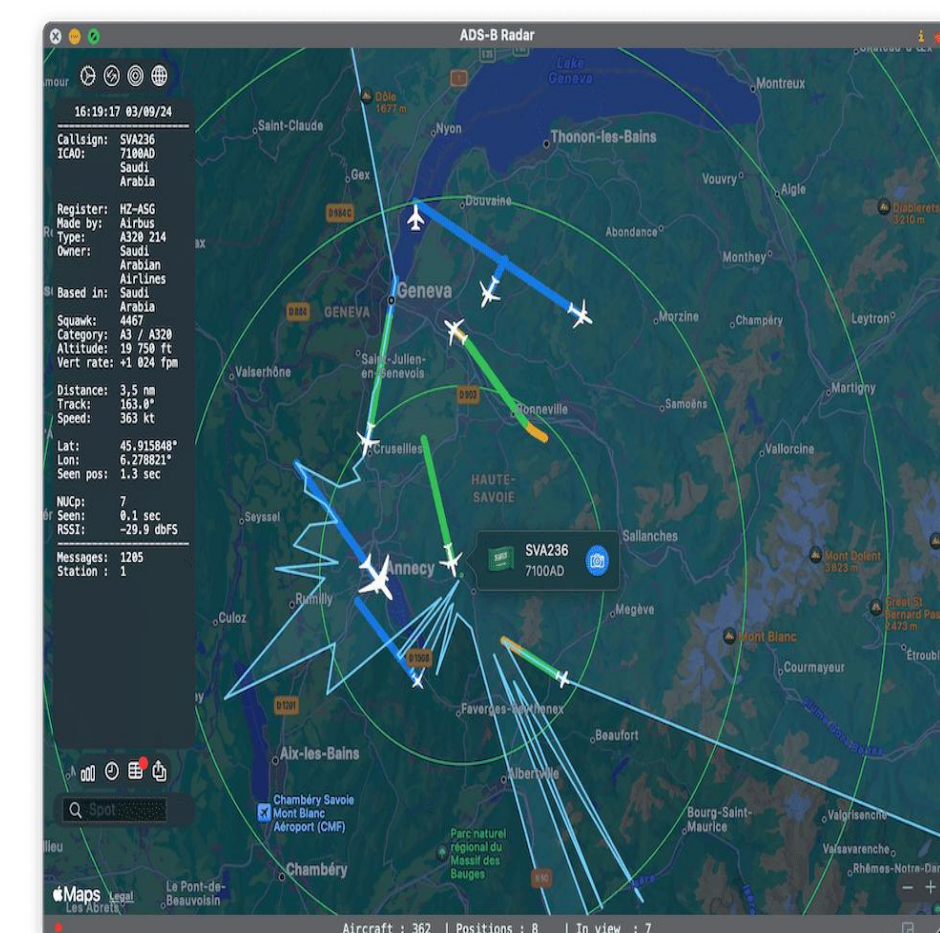
$$c_{ellips} = \frac{1852}{3600 \cdot 1000} \cdot \frac{180}{\pi} \cdot \frac{111}{R}$$

• ϕ = latitude (deg)

• λ = longitude (deg)

• $\hat{\omega}$ = turning rate (rad/s)

$\hat{\omega}$ is inferred from turning patterns found in \mathcal{X} within ϕ_C (for $g_1, \hat{\omega} \approx 0$)



For ADS-B Dynamics

We model aircraft motion using a three-mode physics prior:

$$\mathcal{G} = \{g_{ascend}, g_{level}, g_{descend}\}$$

Aircraft heading $\Delta \psi_i$ and position $\Delta \phi_{km}, \Delta \lambda_{km}$ is predicted using recent contextual detections:

Ground Truth: $\Delta \psi_i = \psi_i - \psi_{i-1}$

Predicted: $\Delta \hat{\psi}_k = \sum w_i \Delta \psi_i$

$$\psi_{eff} = \psi_C + \frac{1}{2} \Delta \hat{\psi}_k$$

$$\Delta \phi_{km} = \frac{v_k \cos(\psi_{eff}) \Delta k}{M(\phi_C) + h_k}$$

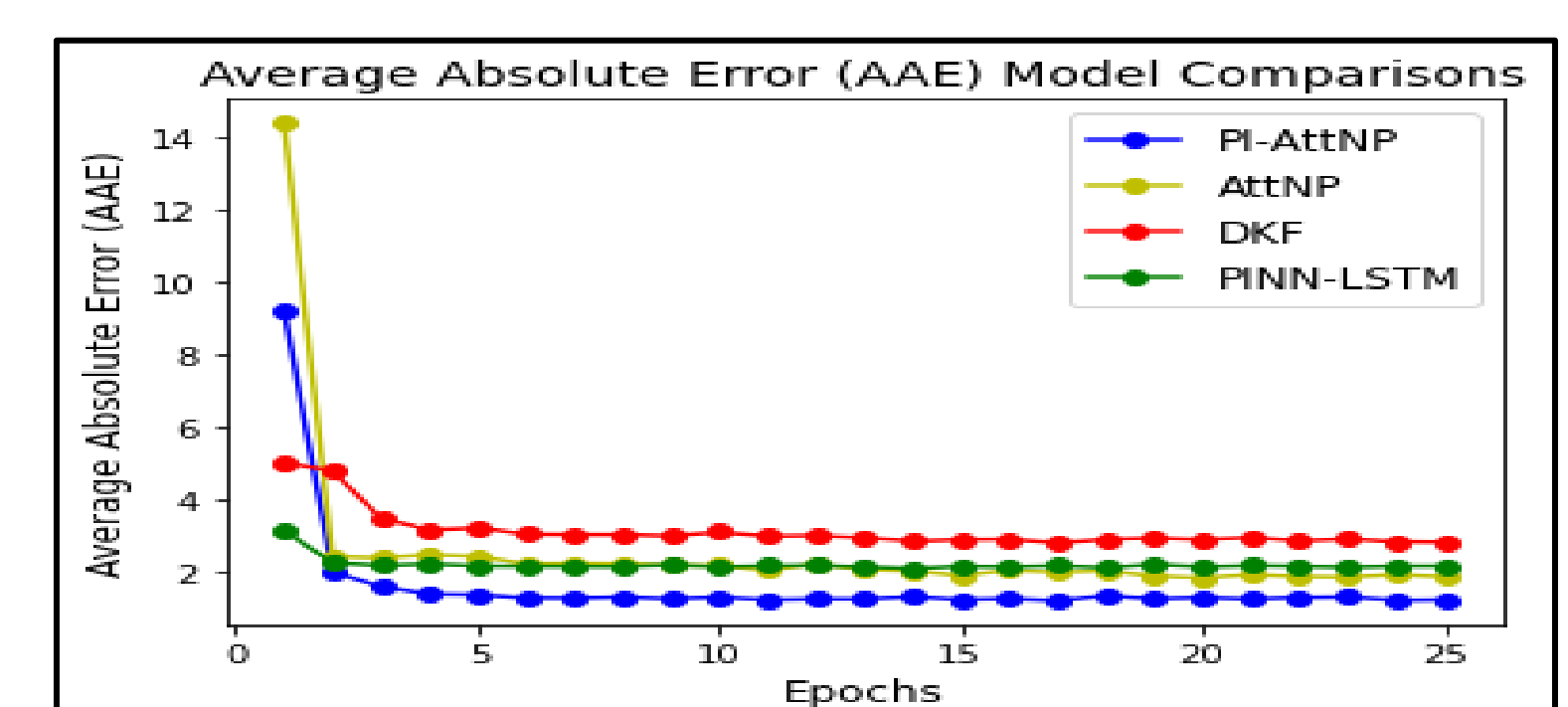
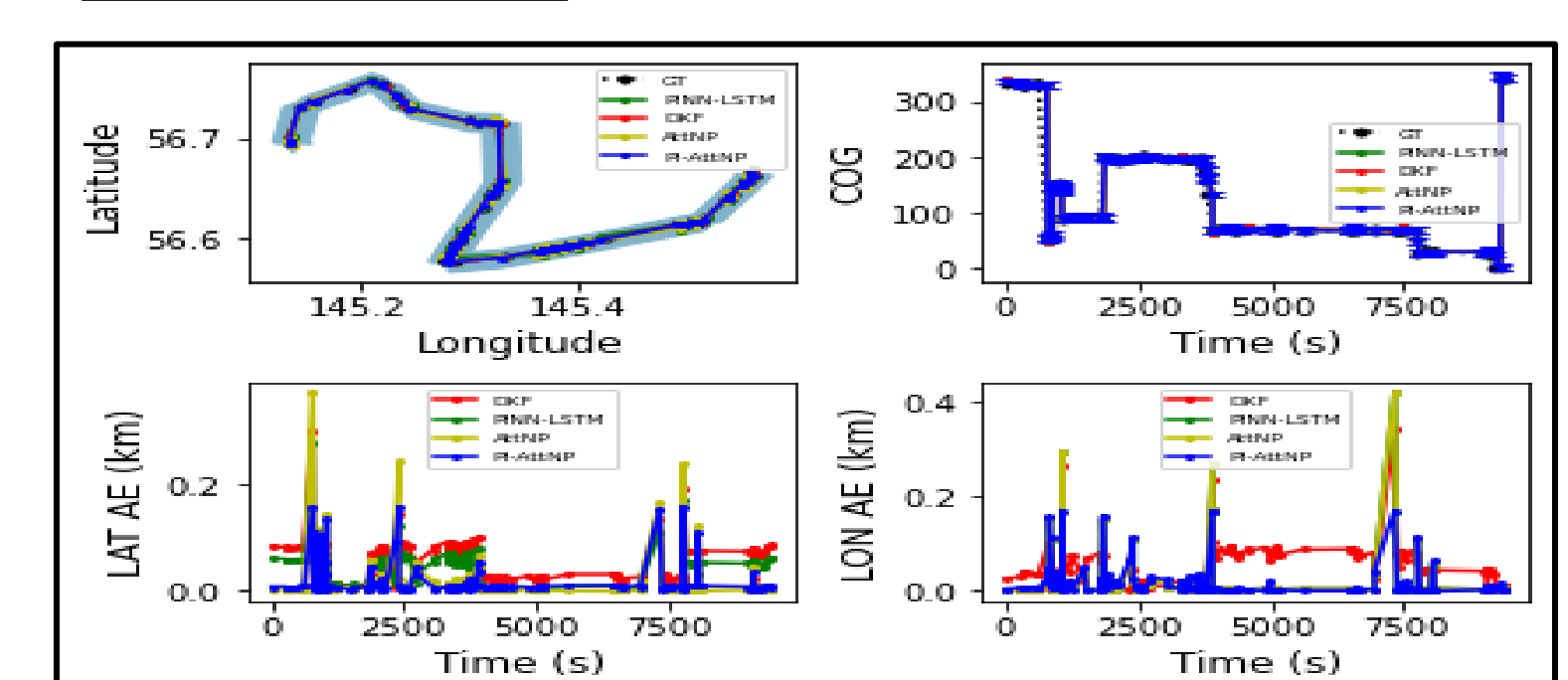
$$\Delta \lambda_{km} = \frac{v_k \sin(\psi_{eff}) \Delta k}{(N(\phi_C) + h_k) \cos(\phi_k)}$$

$$\hat{v}_z = \sum_{i=1}^C w_i \frac{\Delta h_i}{t_i - t_{i-1}}$$

where ψ_{eff} = midpoint heading, M, N = earth radii of ellipsoid, \hat{v} = predicted vertical velocity

RESULTS & DISCUSSIONS

AIS Results



REFERENCES

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